

**Precalc BC      Series, Inductive Proofs and e      Extra Review**

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1. Given a geometric series starting with  $a_n = 1$ , find the range of values to which the series can converge.
  
2. The first and third terms of a sequence are, respectively,  $\frac{3}{4}$  and  $\frac{1}{2}$ . Find the difference between the arithmetic mean and the harmonic mean of these two terms.
  
3. Find the sum of the geometric series:  $17 - 51 + 153 - \dots + 1,003,833$ .

4. Evaluate:      a)  $\sum_{n=2}^{20} 5^n$       b)  $\sum_{n=0}^{\infty} \frac{(-2)^n}{n!}$

5. Given a geometric series with  $r$  a non-real number,  $a_1 = a_4 = 2$ , find  $a_{20} \times a_{21}$ .
  
6. An arithmetic series has  $a_7 = 35$  and  $a_{19} = -1$ . Find the sum of the first 20 terms.

7. The coefficient of the  $x^3y^4$  term of the expansion of  $(2x + ky)^7$  is 672,280. Find the value of  $k$ .

8. Write the first five terms in the expansion of  $\cos(\pi)$ .

9. Prove inductively:  $1 - 2 + 4 - 8 + \dots + (-2)^{n-1} = \frac{1 - (-2)^n}{3}$