Pre Calc BC

3- Difference Quotient

Name_____

1. True or false: $f'(x) = g'(x) \rightarrow f(x) = g(x)$? Give an explanation or a counter example.

- 2. Let $f(x) = 3x^2$
- a) Find f'(4) by making a table with increments of .001 and finding the slope
- b) Find f'(4) by using the limit definition.
- c) Find f'(4) by using nderiv in your calculator.

3. A mathematician takes a walk. Her position (in miles) is given by the equation $s(t) = t - t^4$, where t is time in hours. Graph this equation (use window: $0 \le x \le 1$, $0 \le y \le 1$).

- a) When does she begin to walk back home? (in minutes, please)
- b) How far is she when she turns around?
- c) When does she return home from her walk? (also in minutes)
- d) When is she walking most quickly (minutes)

4. Use nderiv to find the derivative of f(x) = |x| when x = 0. Do you agree with the calculator's answer? (no) What went wrong? What do you think the calculator is doing?

5. Use the limit definition of derivative to find the following:

- a) f'(2), for f(x) = 1/x
- b) g'(-1), for $g(x) = x^2 1$
- c) h'(2), for $h(x) = x^3$

d) Verify these results using either dy/dx in the calc menu or nderiv

- 6. Sketch $f(x) = \sin(x)$.
 - a) Make a sketch of f'(x). Hypothesis?
 - b) Test your hypothesis using n(deriv) on selected values.