## PreCalc BC

## 9- Sketching

## Name:

- 1. Let a particle's position for t > 0 be given by  $s(t) = t^2 + 2/t$
- a) When is the velocity equal to zero?
- b) What is the particle's position at that time?
- c) What is the particle's acceleration at that time?
- d) Is the acceleration ever negative? When?
- e) What is the lower bound of the acceleration?
- 2. Use analytic means to find and classify maxima and points of inflection:

 $f(x) = x^5 - 5x^3 + 3$ . Make a sketch. Verify afterwards with your calculator.

- 3. If you jump out of an airplane without a parachute you fall faster and faster until air resistance causes you to approach a steady velocity called *terminal* velocity.
- a) Sketch a graph of your descent (position) against time.
- b) Explain the concavity of your graph.
- c) Sketch a graph of velocity v. time.
- d) Assuming air resistance to be negligible initially, what natural phenomenon is represented by the slope of your velocity graph at 0 < t < term. vel.
- 4. Put an (a) by all points of inflection if the graph at right is f(x).

Put a (b) by all points of inflection if the graph at right is f'(x).

Put a (c) by all points of inflection if the graph at right is f''(x).

